

PBPK/PD modeling for predicting tumor response

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Motivation PBPK modeling

- To identify the optimal pre-loading for ^{90}Y labeled anti-CD45 antibody (2009)
- To investigate:
 - saturation effects in radioligand therapy (2012)
 - the possibility to predict therapy biokinetics with the PET/CT (2016)
 - the influence of total tumor volume in ^{177}Lu -PSMA therapy (2018)

PBPK = physiologically based pharmacokinetic



Motivation PBPK/PD modeling

- To link the pharmacokinetics with the pharmacodynamics within one model
- To estimate effective radiobiological parameters
- To predict tumor response based on one PET/CT measurement

PBPK/PD = physiologically based pharmacokinetic/pharmacodynamic



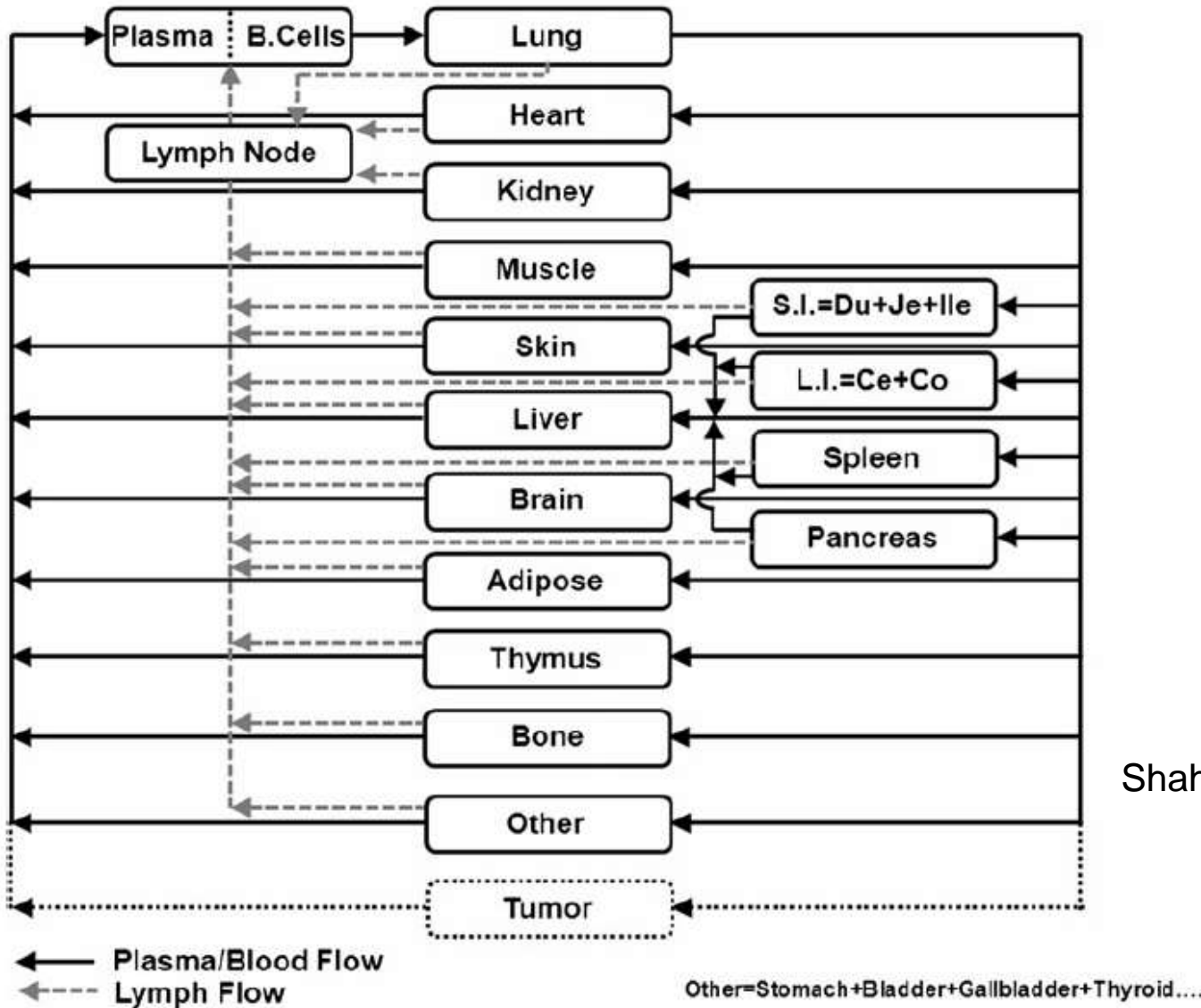
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→ **Big step towards treatment planning**

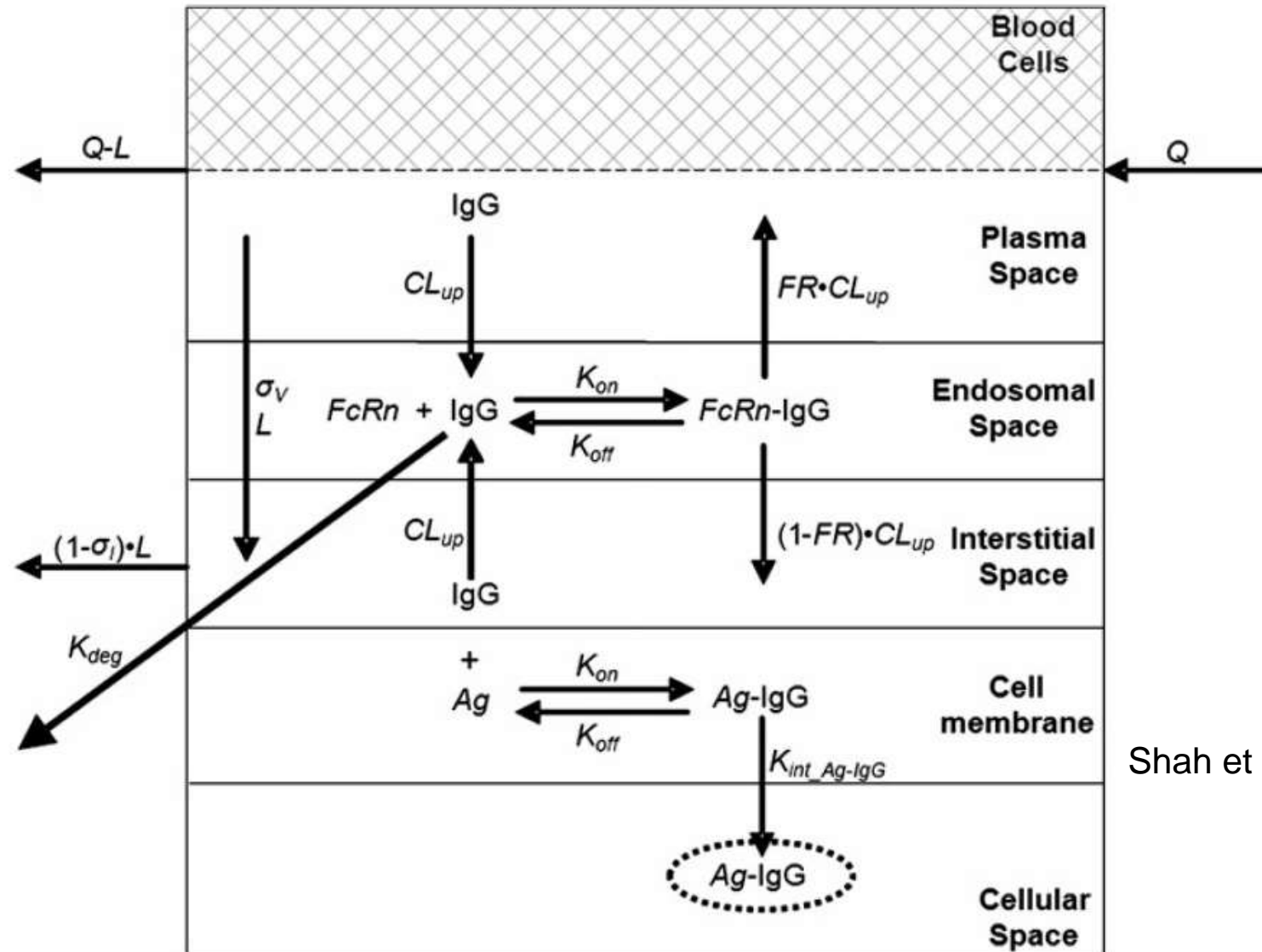


Basic structure of a whole-body PBPK model



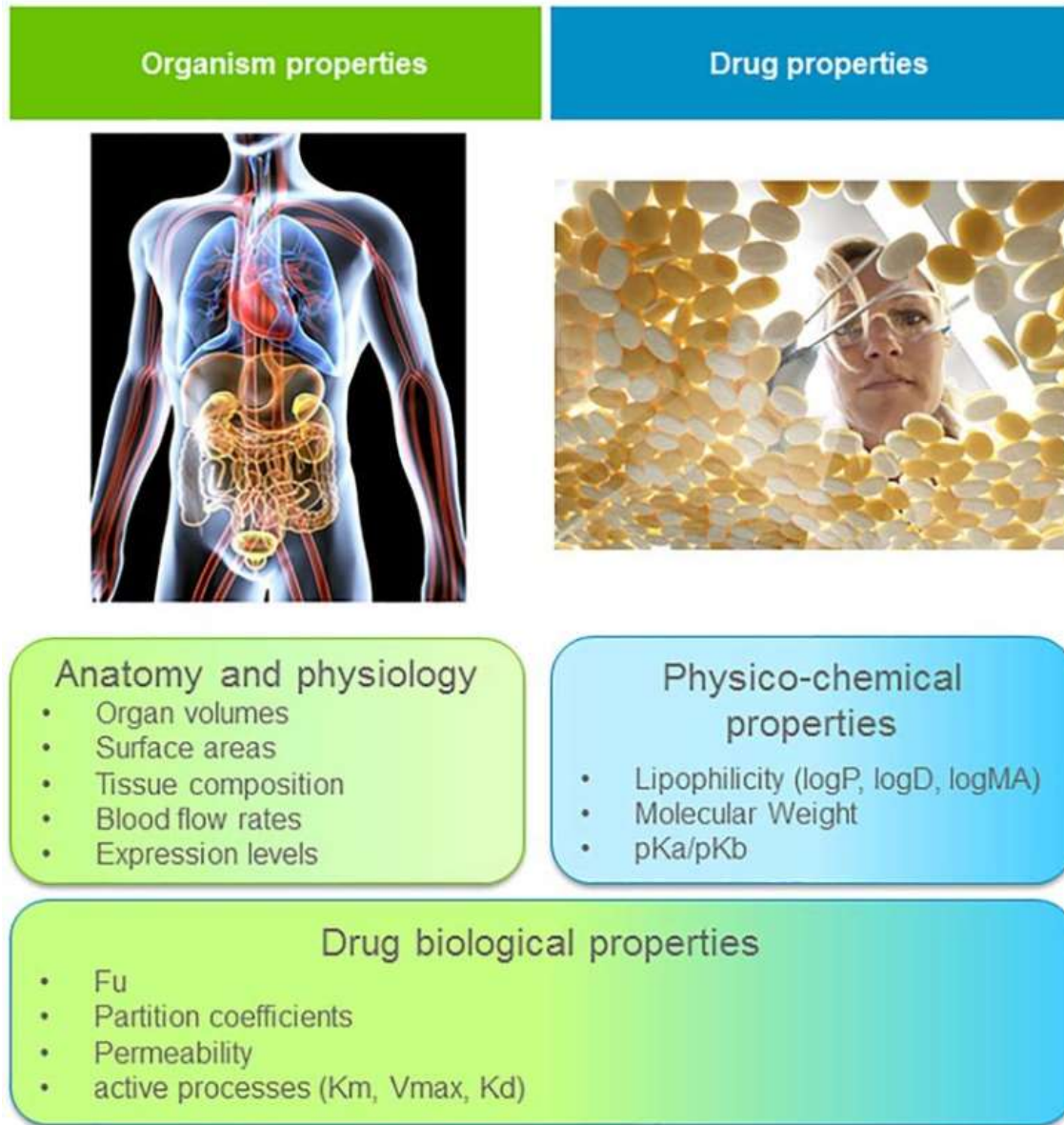
Shah et al. J Pharmacokinet Pharmacodyn 2012

PBPK model organ level for antibodies

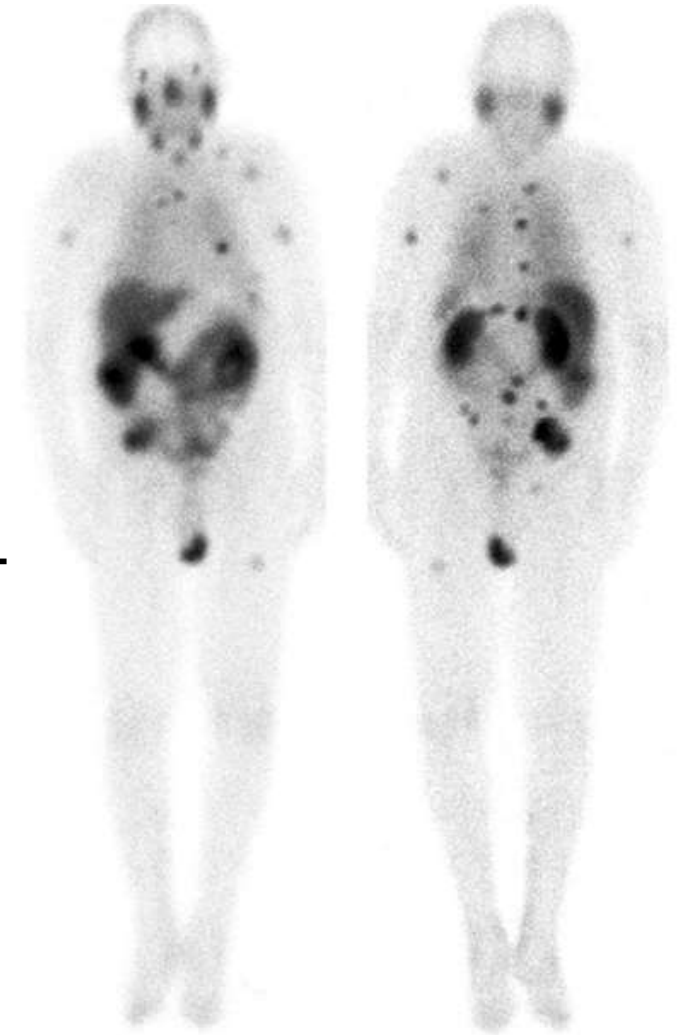


Shah et al. J Pharmacokinet Pharmacodyn 2012

General and individual information

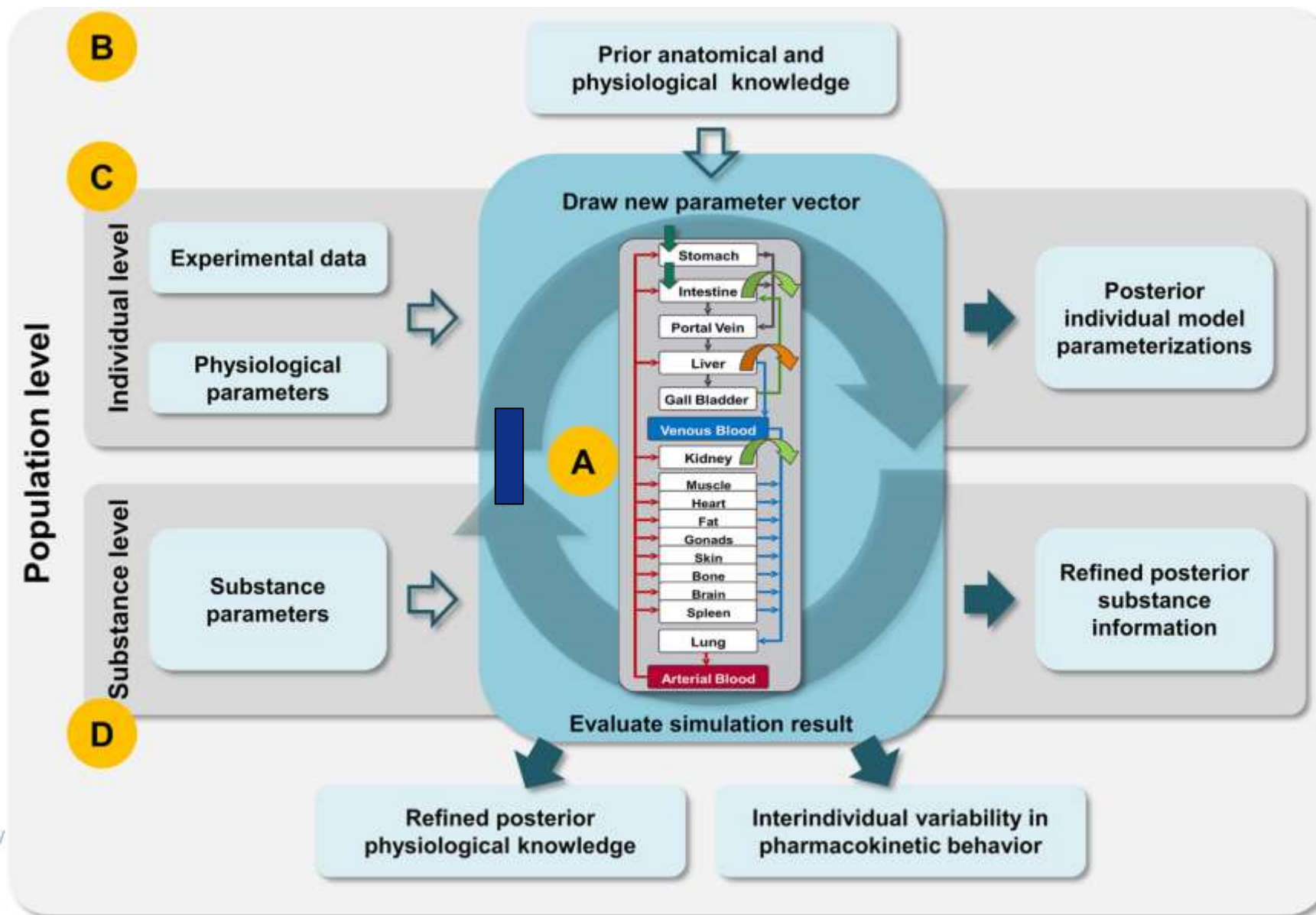


+ Age, BSA, Creatinine... +



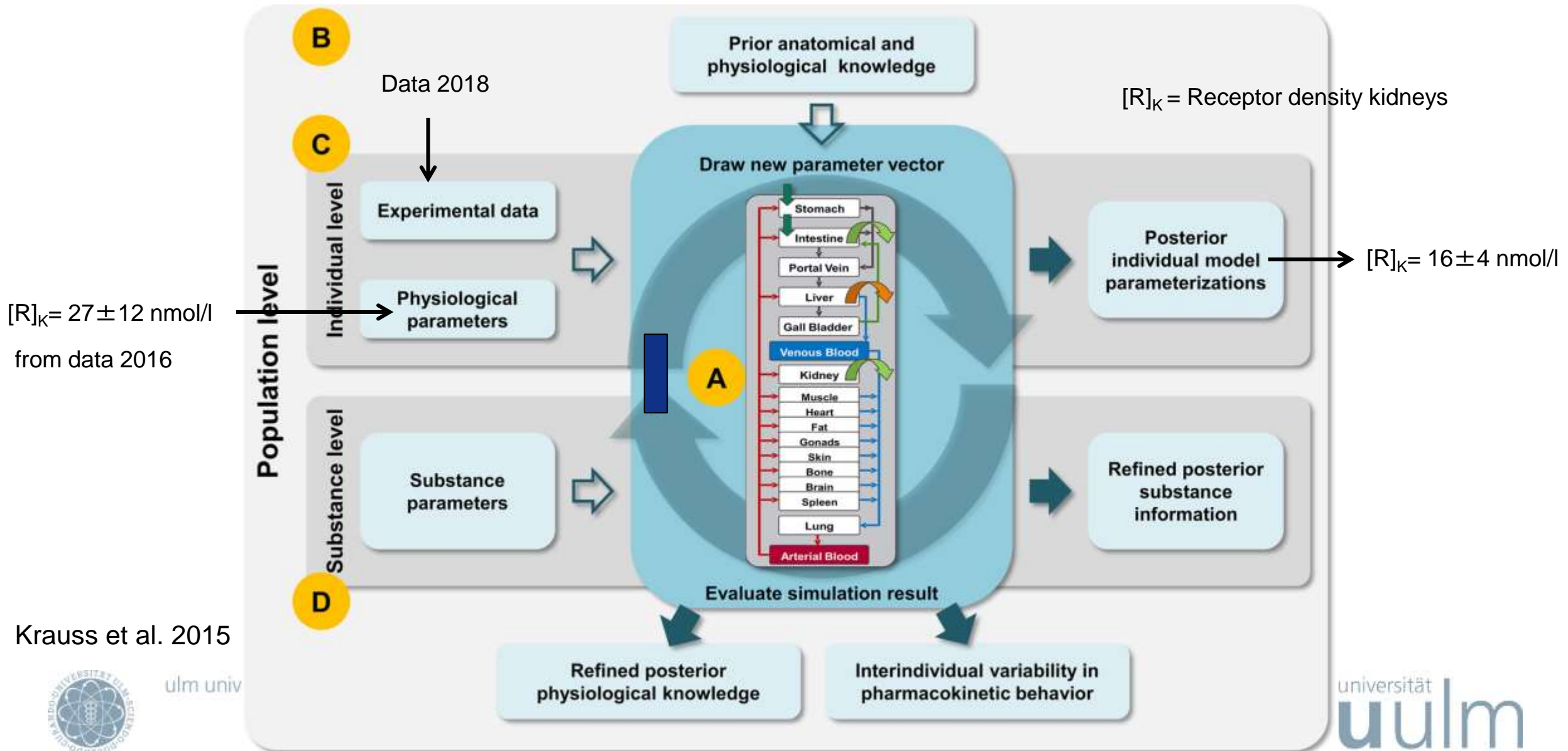
Kuepfer et al. 2016

Integrating information in a Bayesian Framework



Krauss et al. 2015

Integrating information in a Bayesian Framework



Bayesian Framework: Used Objective Function (Sums of Squares)

observation

prior

$$P(\vec{p} | y_i, \text{Gaussian}) = \prod_{i=1}^N \frac{1}{\sqrt{2\pi\sigma_i^2}} \exp\left\{-\frac{(y_i - f(x_i | \vec{p}))^2}{2\sigma_i^2}\right\} \cdot \prod_{j=1}^K \frac{1}{\sqrt{2\pi\omega_j^2}} \exp\left\{-\frac{(p_j - \bar{p}_j)^2}{2\omega_j^2}\right\}$$

$$-2 \ln(P) = \sum_{i=1}^N \left\{ \ln(2\pi\sigma_i^2) + \frac{(y_i - f(x_i))^2}{\sigma_i^2} \right\} + \sum_{j=1}^K \left\{ \ln(2\pi\omega_j^2) + \frac{(p_j - \bar{p}_j)^2}{\omega_j^2} \right\}$$

Measured data point and error

Population mean value
and standard deviation included
as Bayesian information



Advantages of PBPK/PD models

- Simulation of different scenarios using the same basic structure:
 - different amounts of substance
 - different affinities of ligands
- Inclusion of parameters from other experiments/studies:
 - in vitro binding studies and internalisation studies
 - in vivo animal studies → scale up from mouse to human easier
 - physiological and tumour parameters
 - population parameters for a certain patient group
- Less measurements necessary for equal accuracy



Example radioligand therapy using ^{177}Lu -PSMA I&T

- Aim: To develop a method that allows predicting PSMA–positive tumor volume after RLT based on:
- pre-therapeutic PET/CT measurement
 - PBPK/PD modeling



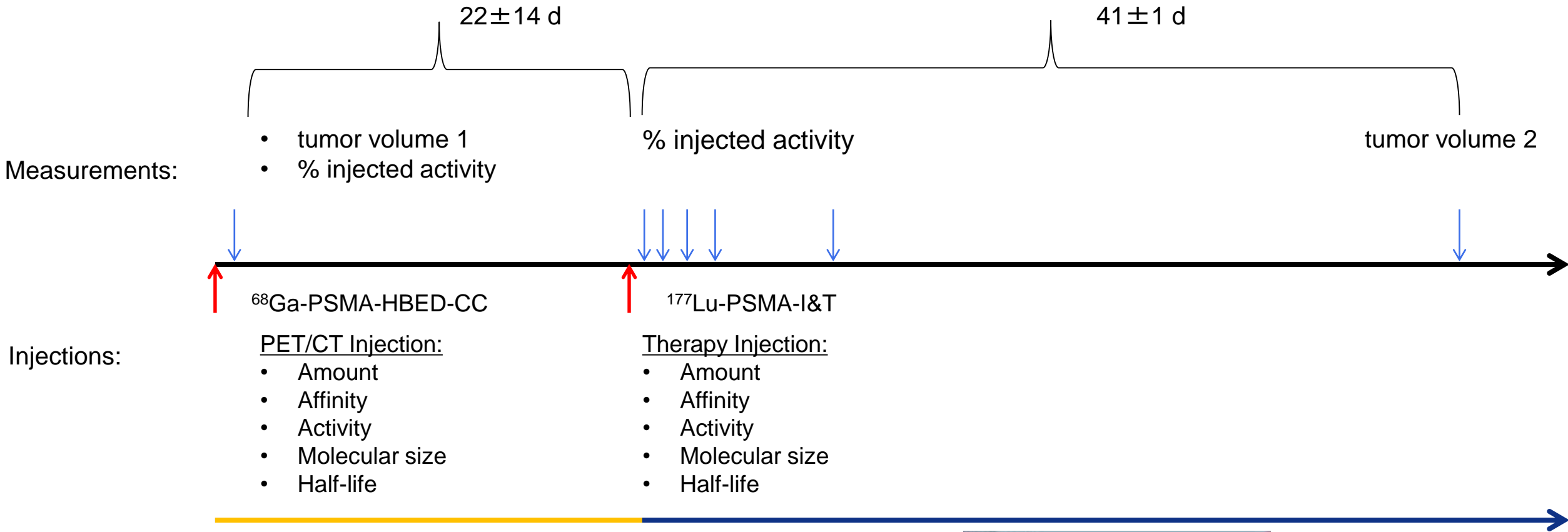
Patient data

For 13 patients with metastatic castration resistant prostate cancer:

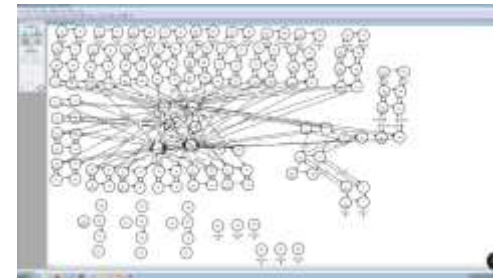
- PET/CT before and after therapy (% injected activity and volumes)
- Planar imaging during therapy
- Time activity data: kidneys, total body, total tumor, 2 tumor lesions per patient
- Basic data (age, activities, amount of peptide,...)



Time line



Switch of related parameters in PBPK/PD model

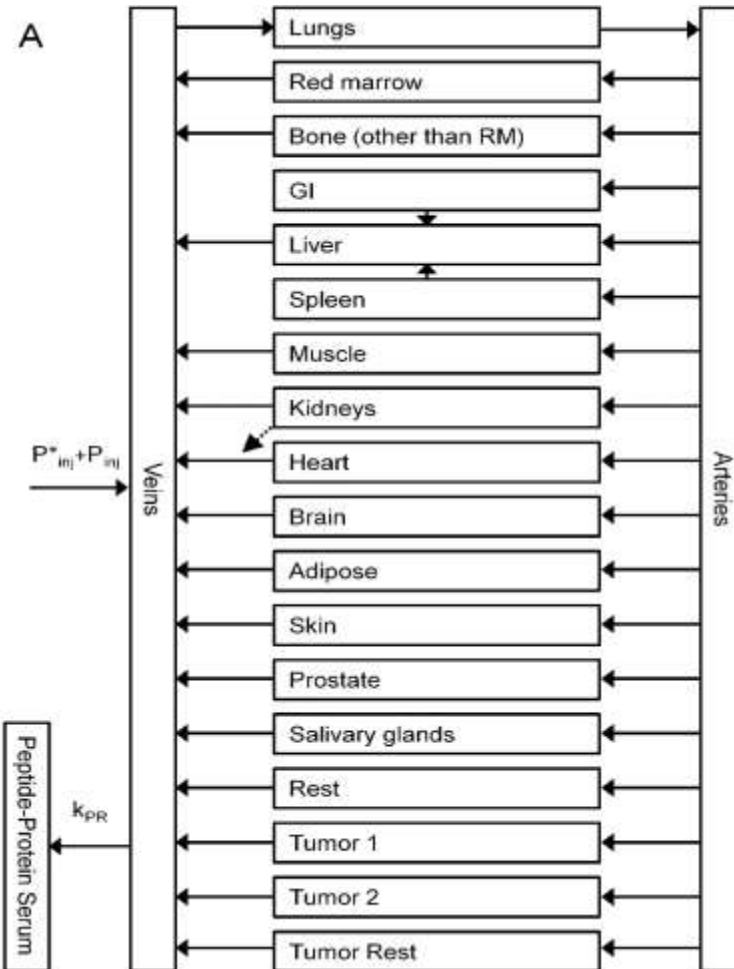


ulm university

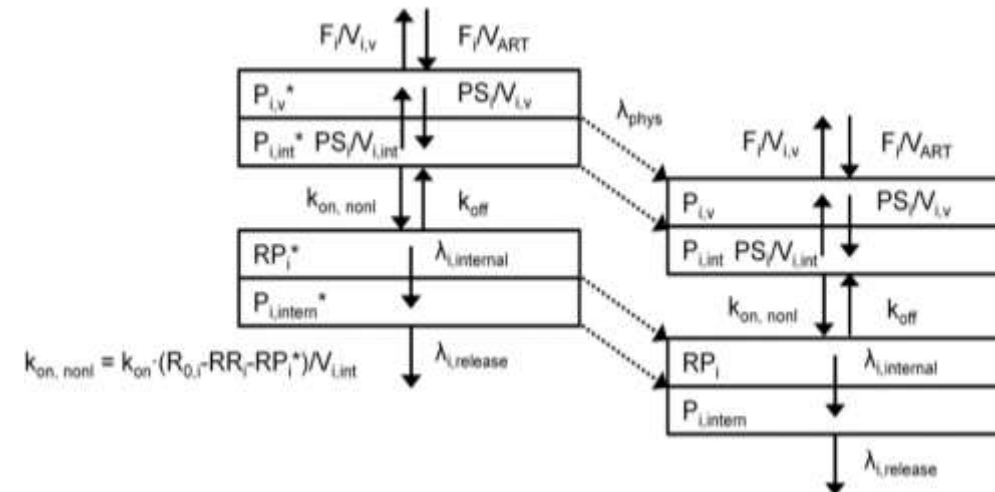


Physiologically Based Pharmacokinetic (PBPK) Model

Global structure



Organ-Level



Kletting *et al.* J Nucl Med. 2016

Tumor growth and dose effect model

$$V_{\text{TU,total}}(t) = V_{\text{TU,total},0} \times e^{(\lambda_g \times t - \alpha_{\text{TU}} \times \text{BED}_{\text{TU}})} \quad \text{Eq. 1}$$

$$\text{BED}_{\text{TU}} = D_{\text{TU}} \times \left(1 + \frac{G_{\text{TU}}}{\alpha_{\text{TU}}/\beta_{\text{TU}}} \times D_{\text{TU}} \right) \quad \text{Eq. 2}$$

$$G_{\text{TU}}(T) = \frac{2}{D_{\text{TU}}^2} \times \int_0^T \dot{D}_{\text{TU}}(t) dt \times \int_0^t \dot{D}_{\text{TU}}(\omega) \times e^{-\mu_{\text{TU}}(t-\omega)} d\omega. \quad \text{Eq. 3}$$

λ_g bone lesions: $5.1 \cdot 10^{-6} \text{ min}^{-1}$;
 λ_g soft-tissue lesions: $3.8 \cdot 10^{-6} \text{ min}^{-1}$

Berges et al.1995

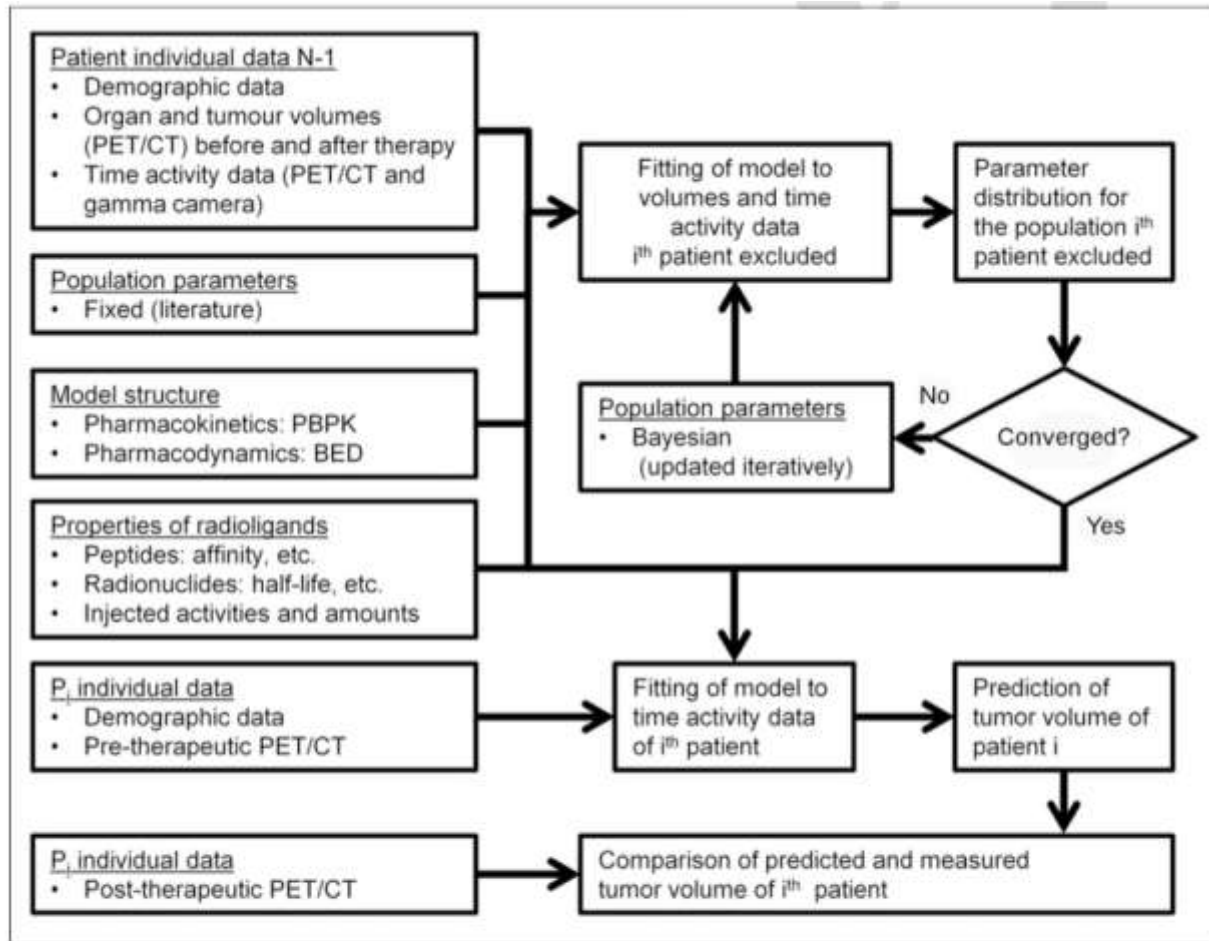
$\alpha_{\text{TU}}/\beta_{\text{TU}} = 1.49 \text{ Gy}$
 $\mu_{\text{TU}} = 0.0061 \text{ min}^{-1}$

Fowler et al. 2001

For the calculation of the absorbed dose, only the self-dose was considered:



Algorithm

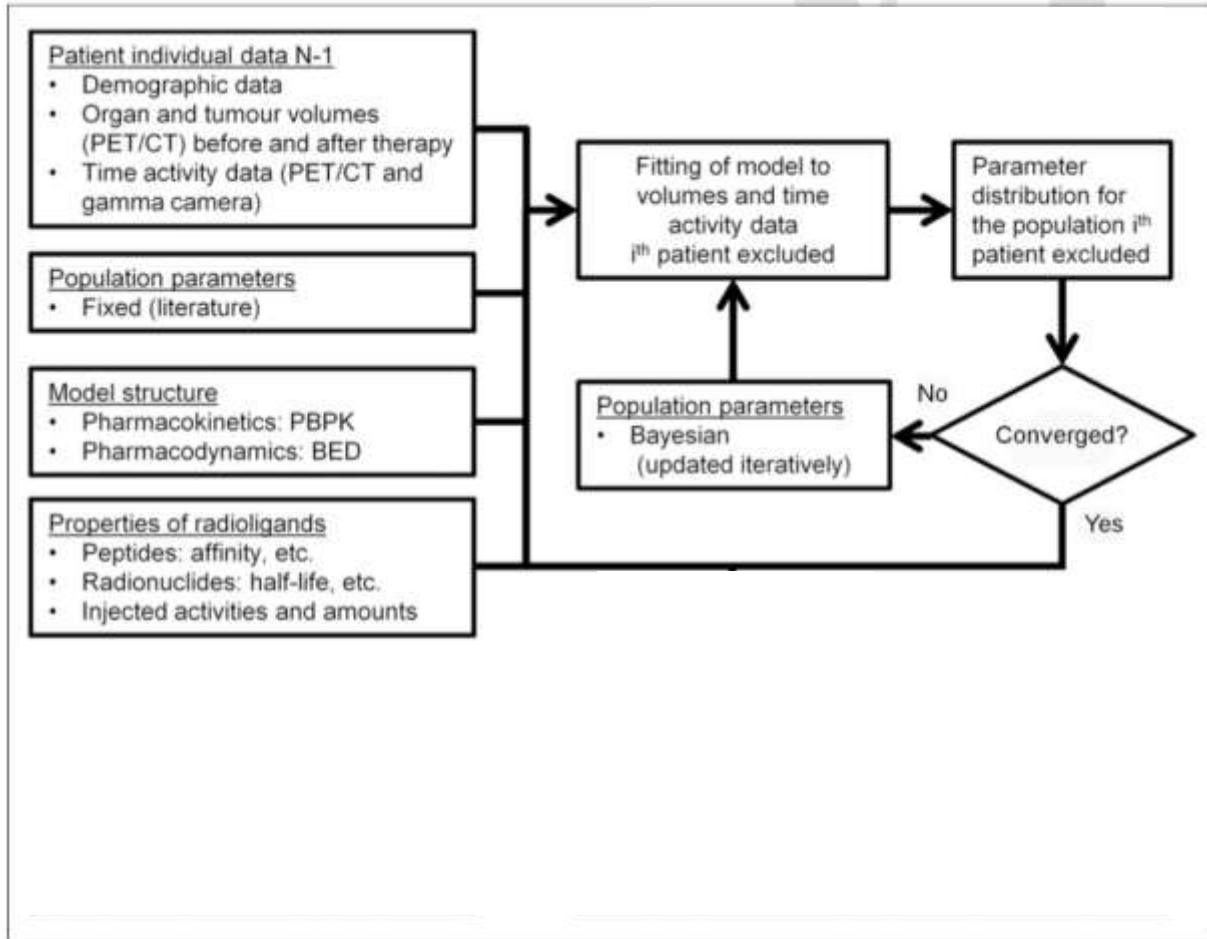


1. Estimation of population values excluding i^{th} patient
2. Fitting with only PET/CT data + Bayesian info
3. Simulation of tumour volumes 6 weeks p.i.
4. Comparison of simulated and measured volumes

Kletting *et al.* J Nucl Med. 2018

FIGURE 1. Model fitting and prediction of tumor volume after treatment. Iterative fitting approach was used to determine Bayesian parameters for investigated population. On the basis of the PBPK model, population parameters (as fixed or Bayesian information) and pretherapeutic PET of excluded patient, volume after treatment was predicted and compared with measured values. This was conducted for all ($n = 13$) patients.

1. Estimation of populations values

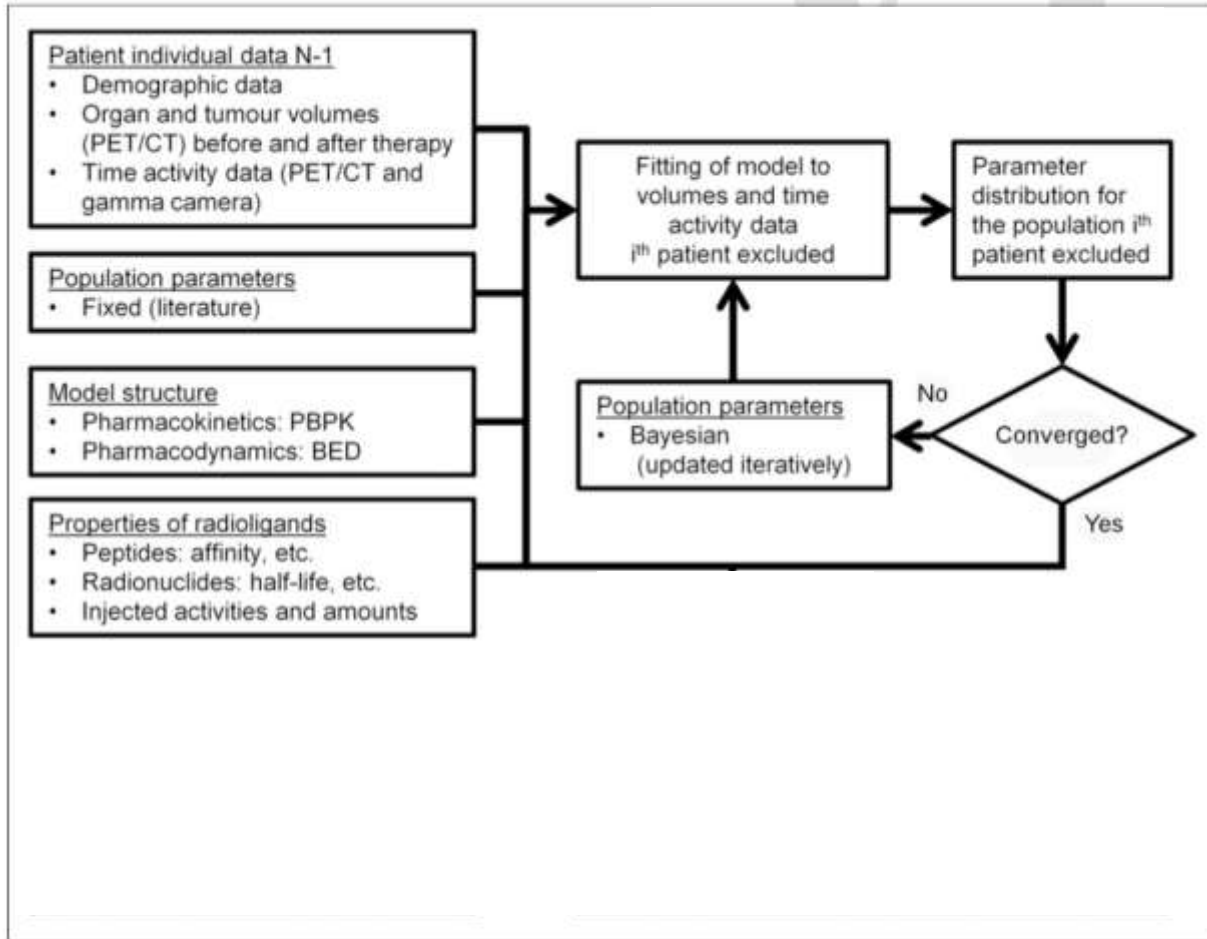


For each patient:
Estimation of population values
leaving out the data of just this patient

- For tumor and kidneys:
- receptor densities
 - blood flows per g
 - release rates from tissues
 - radiosensitivity

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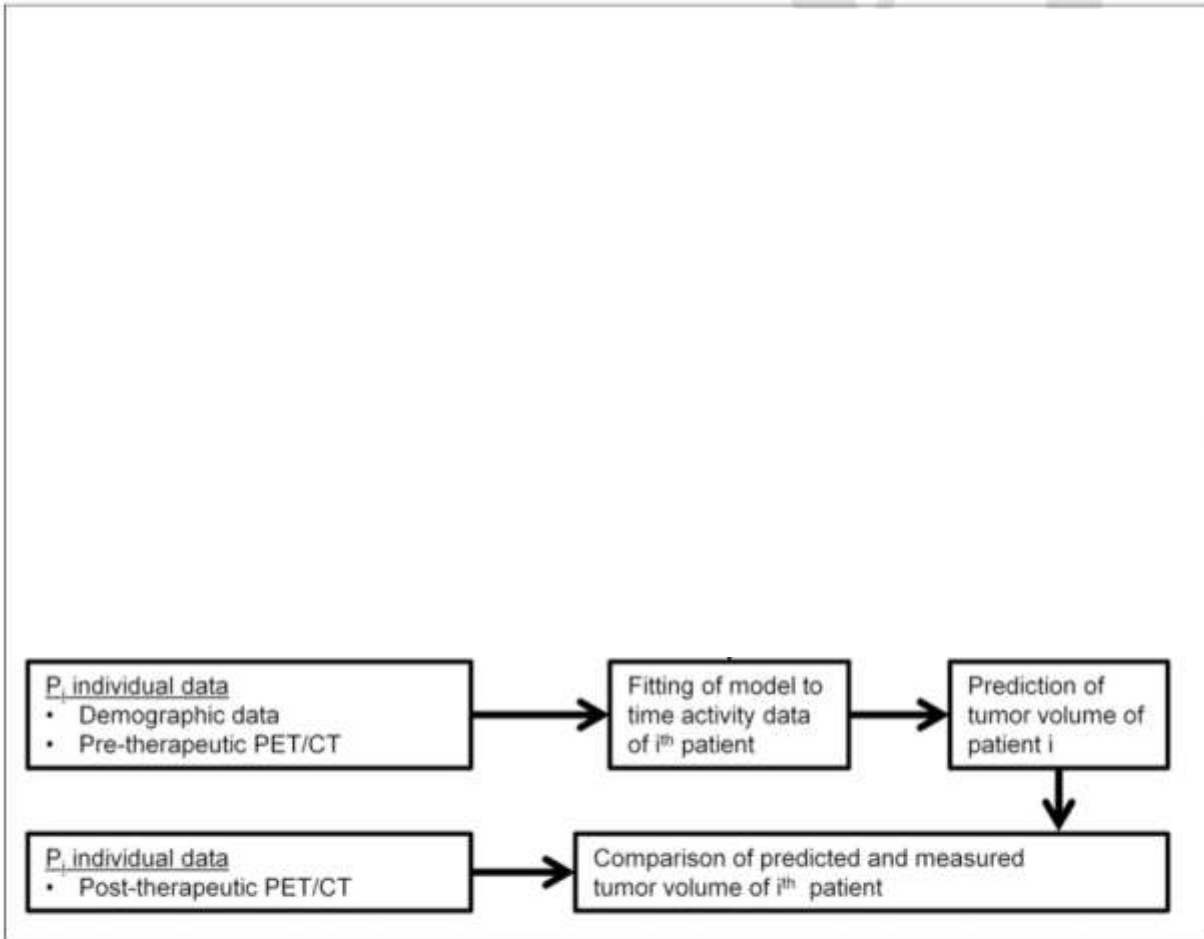


For example:

$$\alpha_{TU} = 0.0172 \pm 0.0084 \text{ Gy}^{-1}$$

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2. Fitting with only PET/CT data + Bayes population values



Fixed parameters:

- radiosensitivity
- release rates

Fitted with Bayesian term:

- receptor densities
- blood flows

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3. Simulation of therapy and post therapy tumor volumes

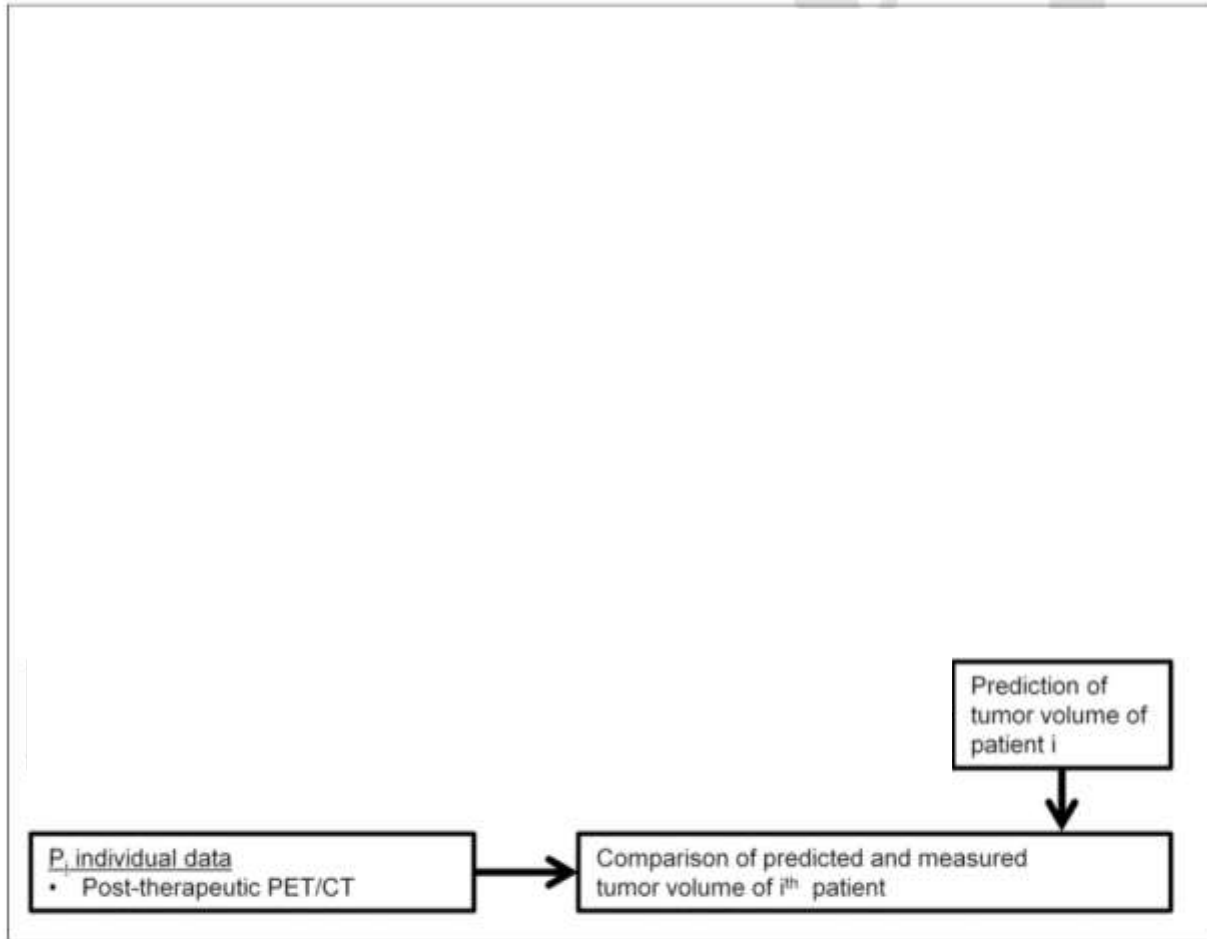


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4. Comparisons of predicted and measured tumor volumes

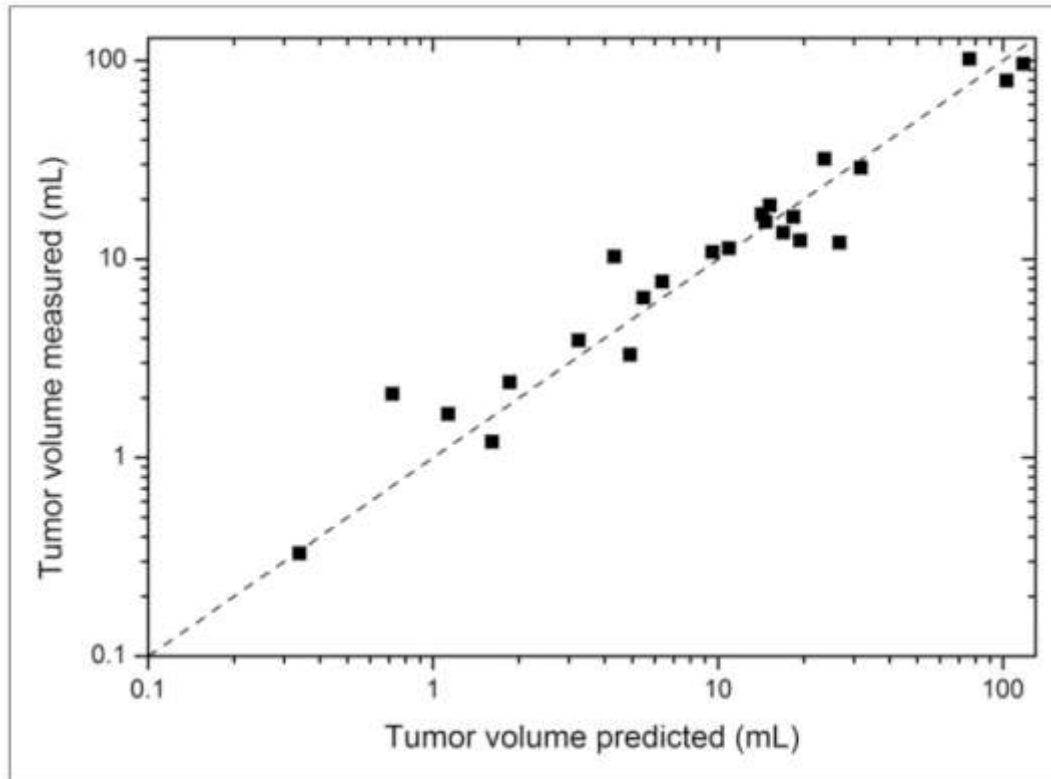


FIGURE 2. Predicted versus measured tumor volume. Prediction is based on PBPK/PD model, pretherapeutic measurement, and population parameters.

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$$RD_{TU,volume} = \frac{V_{TU,total,0} \times e^{(\lambda_g \times t_{PETCT2} - \alpha_{TU} \times BED_{TU})} - V_{TU,total,PETCT2}}{V_{TU,total,PETCT2}} \times 100\% \quad \text{Eq. 6}$$

$$RD_{TU,volume} = 1\% \pm 40\%,$$

Improvements

Model

- Better tumor growth (power-law) and dose effect model (different states of cells)

Data

- Including SPECT/CT data and more patients
- More accurate and automated estimation of total tumor volume

Methods

- Identification of subpopulations (smaller standard deviations of the Bayesian terms)
- Integration of PSA values as *a priori* information. How?
- Complete uncertainty analysis



Acknowledgement



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Behnken-Berger Stiftung



Probability distributions

